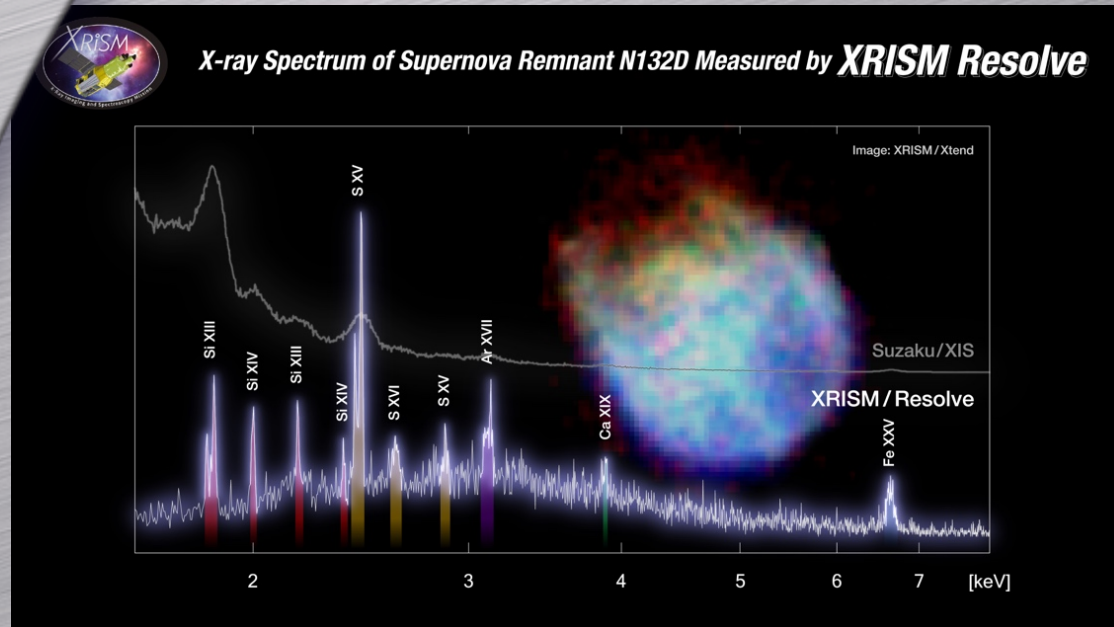


Improving Theoretical Charge Exchange Cross Sections for Astrophysical X-ray Emission Modeling: **Limitations and Future of Kronos**

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Collaborators



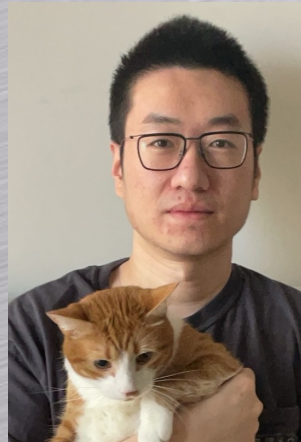
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Renata
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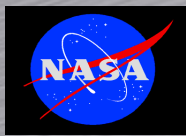
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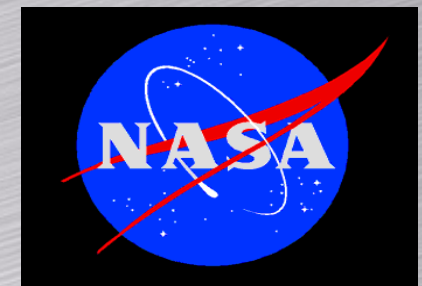
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Funding:
NASA APRA
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Outline

- Introduction
- CX Theoretical Methods Overview
- The Kronos Database/Spectra Model
- Other CX Databases
- Examples - importance of Double Capture
- Summary
- The Future

CX Cross Section Theory

- n -, l -, L -, and S -resolved cross sections are needed for ~ 10 eV/u to ~ 10 MeV/u

- Various methods used:

- Lattice time-dependent Schroedinger equation (LTSE)

- Quantum molecular-orbital close-coupling (QMOCC)

- Atomic-orbital close-coupling (AOCC)

- Classical-trajectory Monte Carlo (CTMC)

- Multichannel Landau-Zener (MCLZ)

Accuracy



Computational Effort

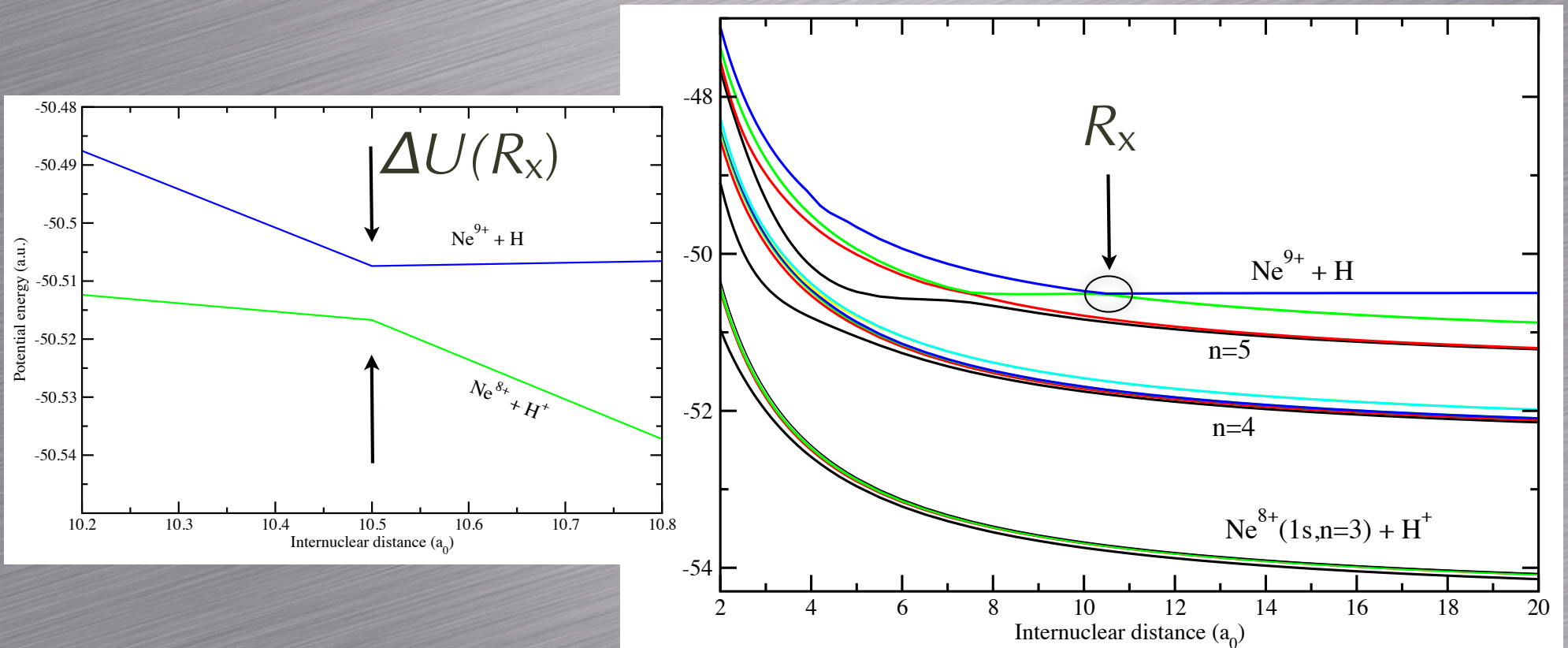


Multichannel Landau-Zener

- Janev, McDowell, & Bransden (1983); Butler & Dalgarno (1980); Gershstein (1963)
- N-channels — almost unlimited
- LZ parameters: 1) avoided-crossing distances (R_x), 2) potential energy difference at R_x [$\Delta U(R_x)$], and 3) the difference in diabatic potential slopes at R_x [$F(R_x)$]
- R_x - from asymptotic atomic energies (NIST) and IPs
- $F(R_x)$ - model potential functions w/polarizabilities
- Problem: bare-ion cases give only n -resolved cross sections → l -distribution functions must be used

Multichannel Landau-Zener

- Largest uncertainty from $\Delta U(R_x)$
- Various models for $\Delta U(R_x)$: one-electron (Olson-Salop 1977), multi-electron (Taulbjerg 1986), low-charge (Butler-Dalgarno 1980)



l-distributions from CX

- Model *l*-distribution functions often used:

- 1. **Low-energy** (Landau-Zener)
(< 1 keV/u?) \rightarrow

$$\frac{(2l + 1)(n - 1)!}{(n + l)!(n - l - 1)!}$$

- 2. Low-energy II (< 1 keV/u?)

- 3. Separable (< 1 keV/u?)

- 4. Flat (**even**) (1-10 keV/u?) - all *l* cross sections equal

- 5. **Statistical** (> 10 keV/u?) \rightarrow

$$\frac{(2l + 1)}{n^2}$$

- Required for bare-ion MCLZ calculations only (H-like emission)



The Kronos CX Database

(sites.physast.uga.edu/ugacxdb)



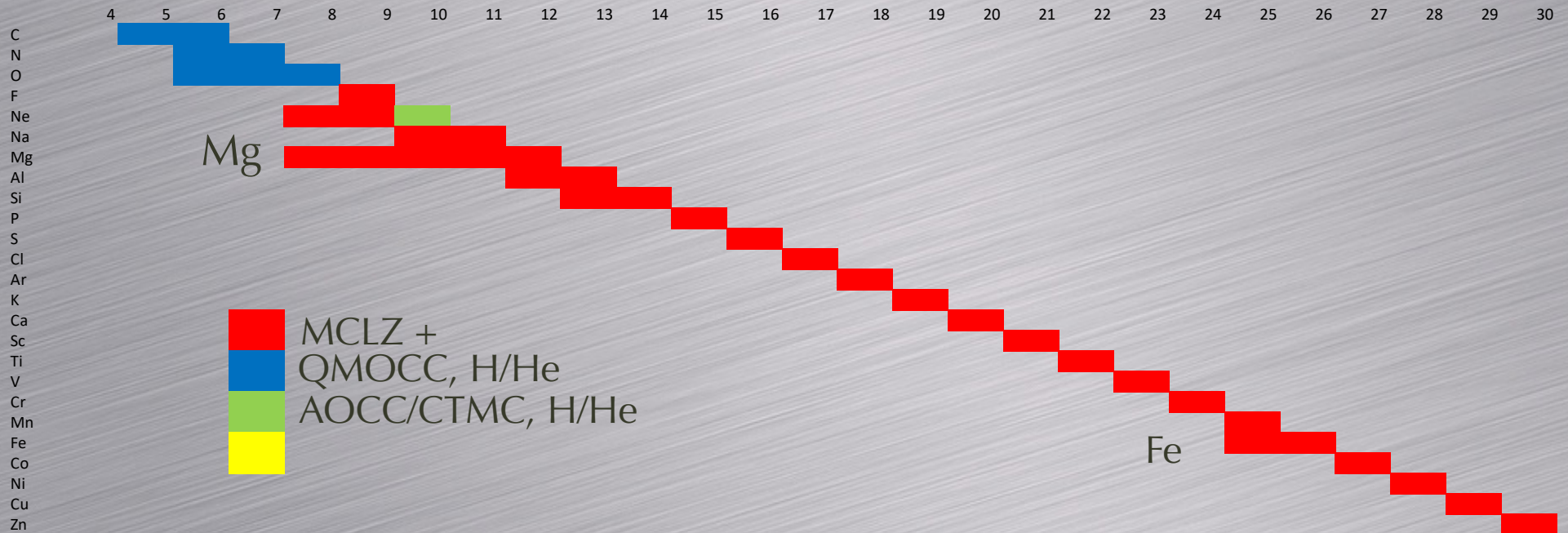
● First version (2017-2019):

- Database of *Single Electron Capture* (SEC) cross sections, ion energies and A-values (NIST, analytical, and Autostructure), and cascade/X-ray spectrum model
- Mostly MCLZ results, but also QMOCC, AOCC, CTMC, “recommended”
- Ions: H-like C-Zn, He-like C-Si
- Neutral targets: H, He, H₂, N₂, H₂O, CO, CO₂, some cross sections for O, OH, Kr

Mullen et al. 2016, ApJS, 224, 31; 2017, ApJ, 844, 7

Cumbee et al. 2019, ApJ 852, 7

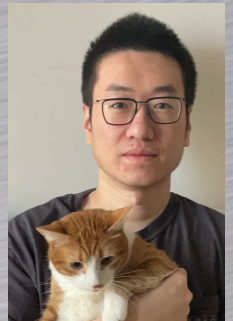
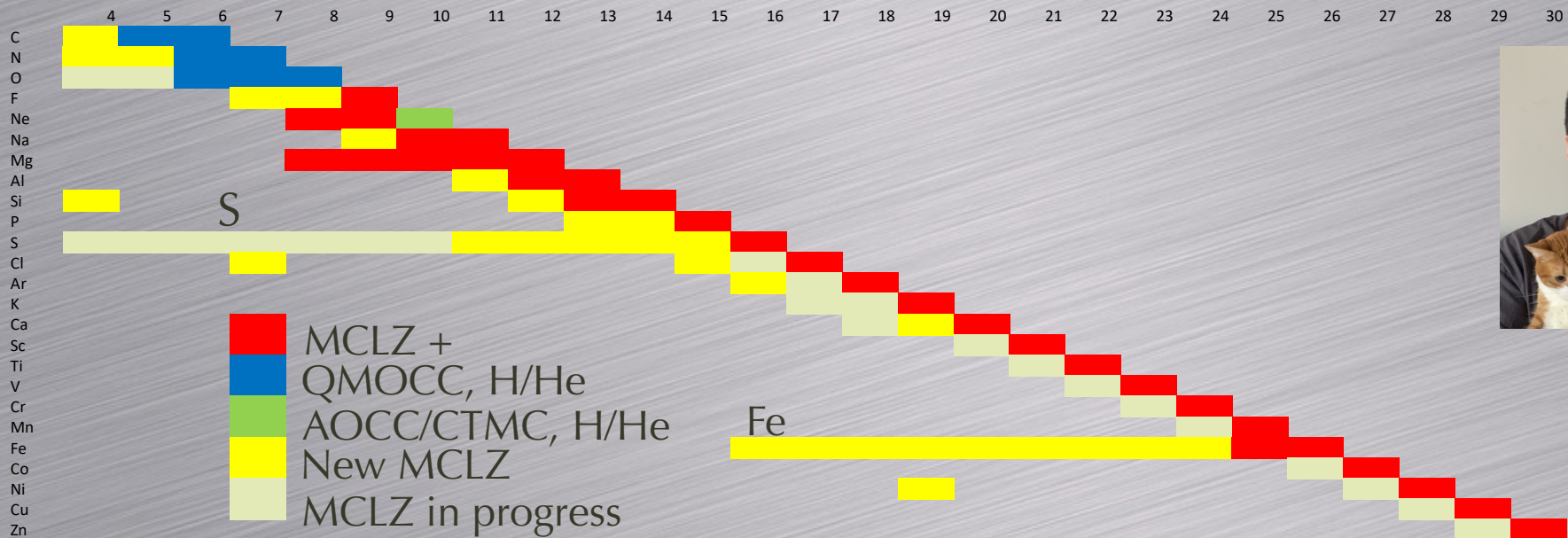
Current Kronos (v3.1)



The Kronos CX Database

- **New version (Fall 2024):**
 - He-like ions (P-Zn)
 - All Li-like ions (C-Zn)
 - Additional targets: CH₄, NH₃
 - Multielectron ions: C, O, Ne, S, Mg, and Fe
 - Complex atomic structure: $n, l, L, 2S+1$, seniority
 - GUI
 - More literature data
 - Data provenance

Next Kronos



Not pictured:
Lior Shefler
Sean McIlvane



Kronos GUI



The image shows two overlapping windows of the Kronos GUI. The top window is titled "KRONOS CX DATABASE" and displays the "O8+ CX with CO: mclz_nres method" plot. The plot shows cross-sections on a logarithmic scale (y-axis, from 10^{-25} to 10^3) versus collision energy in eV/u (x-axis, from 10^{-2} to 10^5). The plot includes curves for $n=7$ (red), $n=6$ (blue), $n=5$ (purple), $n=4$ (grey), $n=3$ (orange), $n=2$ (green), $n=1$ (pink), and Total (black). The control panel for this window shows: Ion: O, Neutral: H2O, Method: mclz, Collision Energy (eV/u): 1000, Range: 0.001-100000.0 eV/u, Minimum Energy: 10.0, Maximum Energy: 1000.0, Energy Resolution: 5.0, Smooth Points: 2000, and a checked "Gaussian" option. The bottom window is also titled "KRONOS CX DATABASE" and displays the "O7+ CX with H2O: mclz method" plot. The plot shows relative intensity in arbitrary units (y-axis, from 0.0 to 20.0) versus photon energy in eV (x-axis, from 500 to 750). The control panel for this window shows: Ion: O, Neutral: CO, Method: mclz_nres, Collision Energy (eV/u): 1000, Range: low-energy, Minimum Energy: 10.0, Maximum Energy: 1000.0, Energy Resolution: 5.0, Smooth Points: 2000, and a checked "Gaussian" option. The background shows a macOS desktop with various application icons and a dock.

• Beta testing in progress

• Jupyter notebooks in progress - comparison to ACX, SPEX, NIST thermal spectra

Kronos Details

- **What Kronos does:**

- MCLZ: l -distribution models for H-like ions only
- 2+ electrons, no l -distribution needed
- MCLZ, QMOCC: no assumed triplet-singlet ratio

- **What Kronos doesn't do:**

- Fine-structure-resolved cross sections (*coming soon*)
- Multiple electron capture (*only single electron capture*)

- **Coming soon (2 NASA APRA grants):**

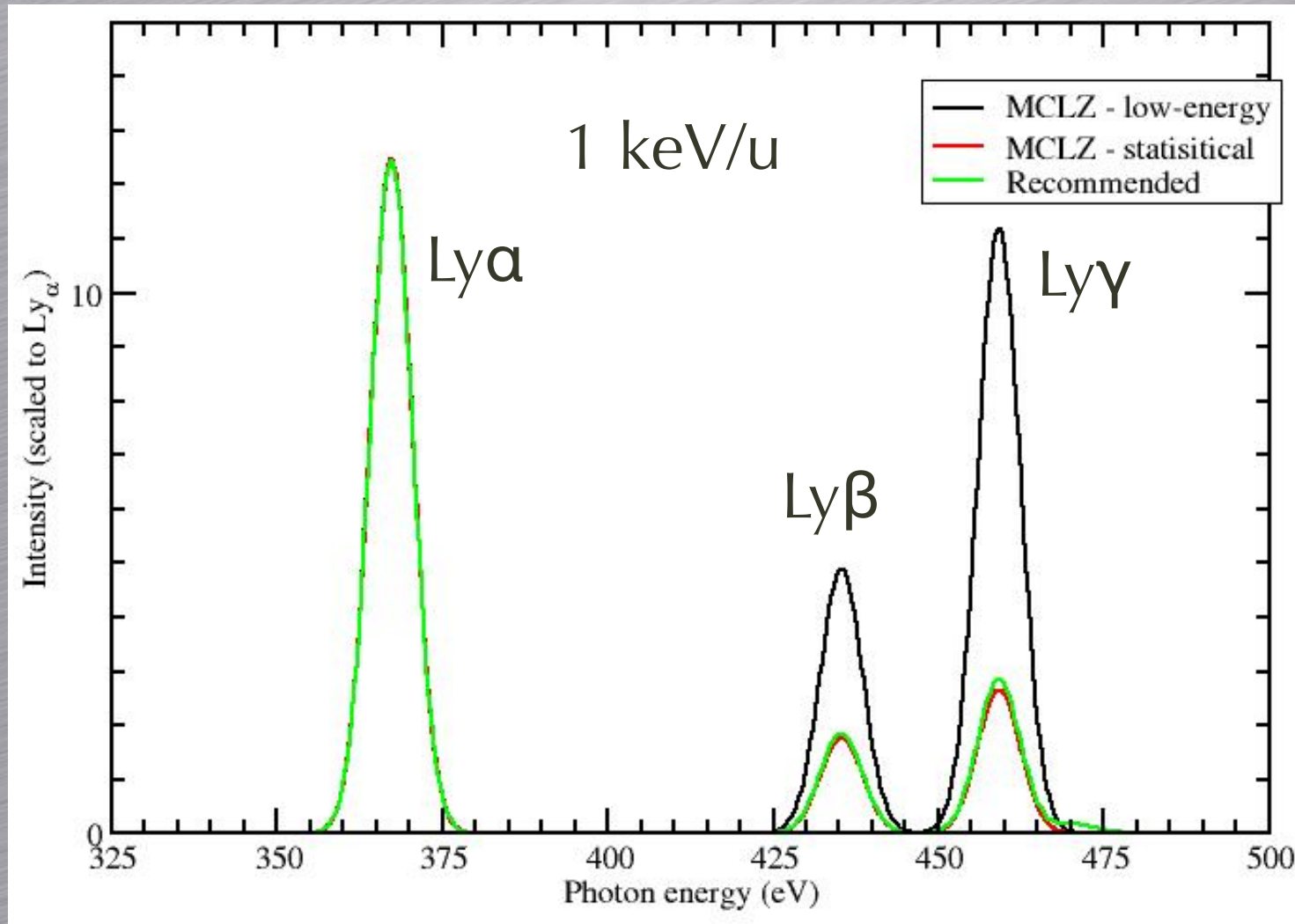
- QMOCC pipeline calculations (nearly exact 1-electron)
- Two-electron AOCC code
- Benchmarking to EBIT and other measurements
- Machine learning optimization to improve MCLZ

CX Databases

- **AtomDB: AtomDB Charge Exchange (ACX v1) model:**
 - Classical over-the-barrier (COB) model, 2 parameters: q , IP of neutral
 - Predicts total CX cross section, dominant n ; no velocity dependence
 - l -distribution models, triplet-singlet ratio = 3
 - ACX v2: ingested *Kronos* data, ACX v1 for systems not in *Kronos*
- **SPEX:**
 - Fits of existing experimental data
 - Ingested *Kronos* data
- **Flexible Atomic Code (FAC)**
 - Ingested *Kronos* data
- Also **xstar and Cloudy** -> mostly total rate coefficients

Examples

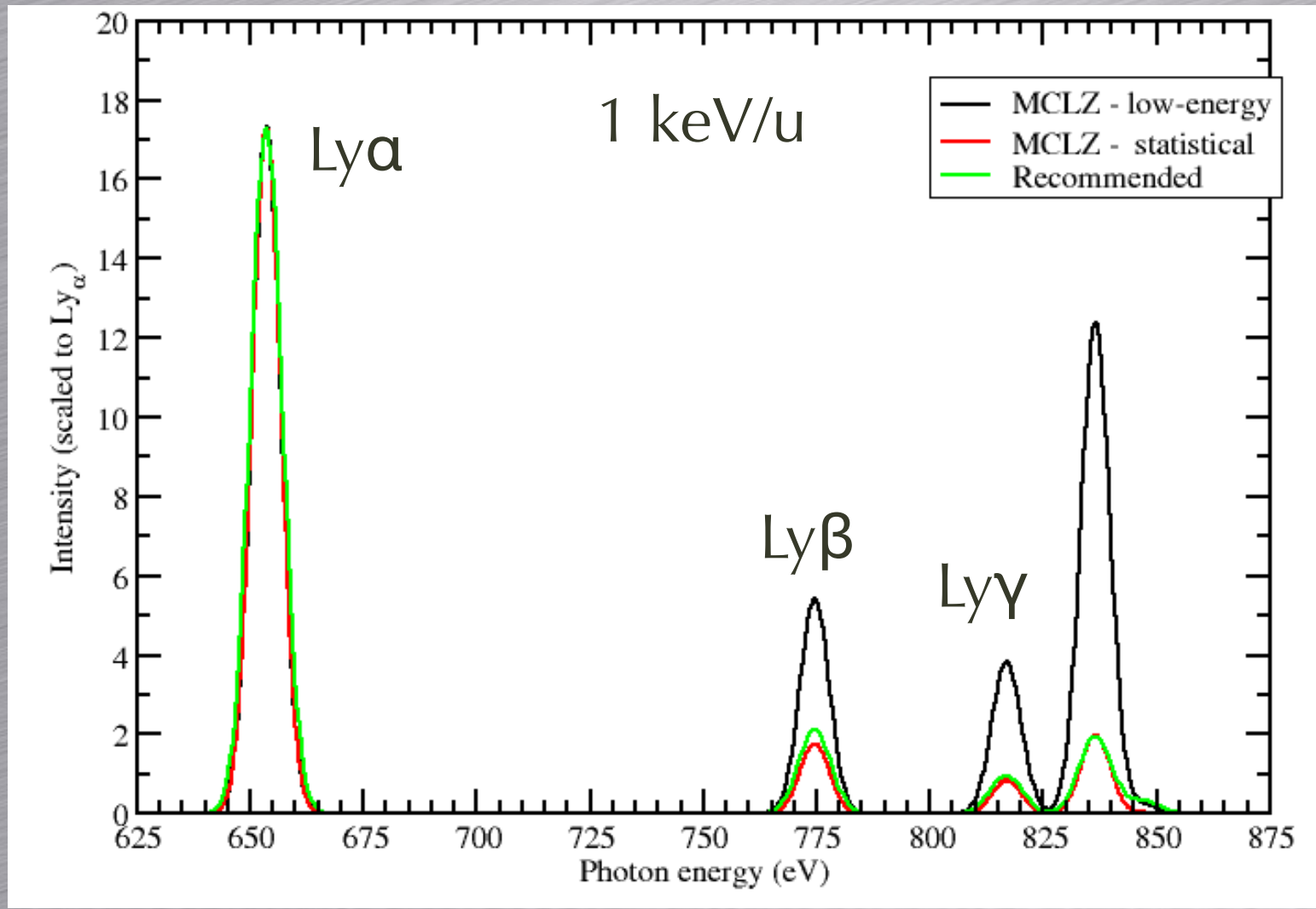
X-ray Spectra for $C^{6+} + H$ comparison



4.5 eV
resolution
Cumbee et al.
(2019)

Recommended: Janev et al. 1993, ADNDT, 55, 201

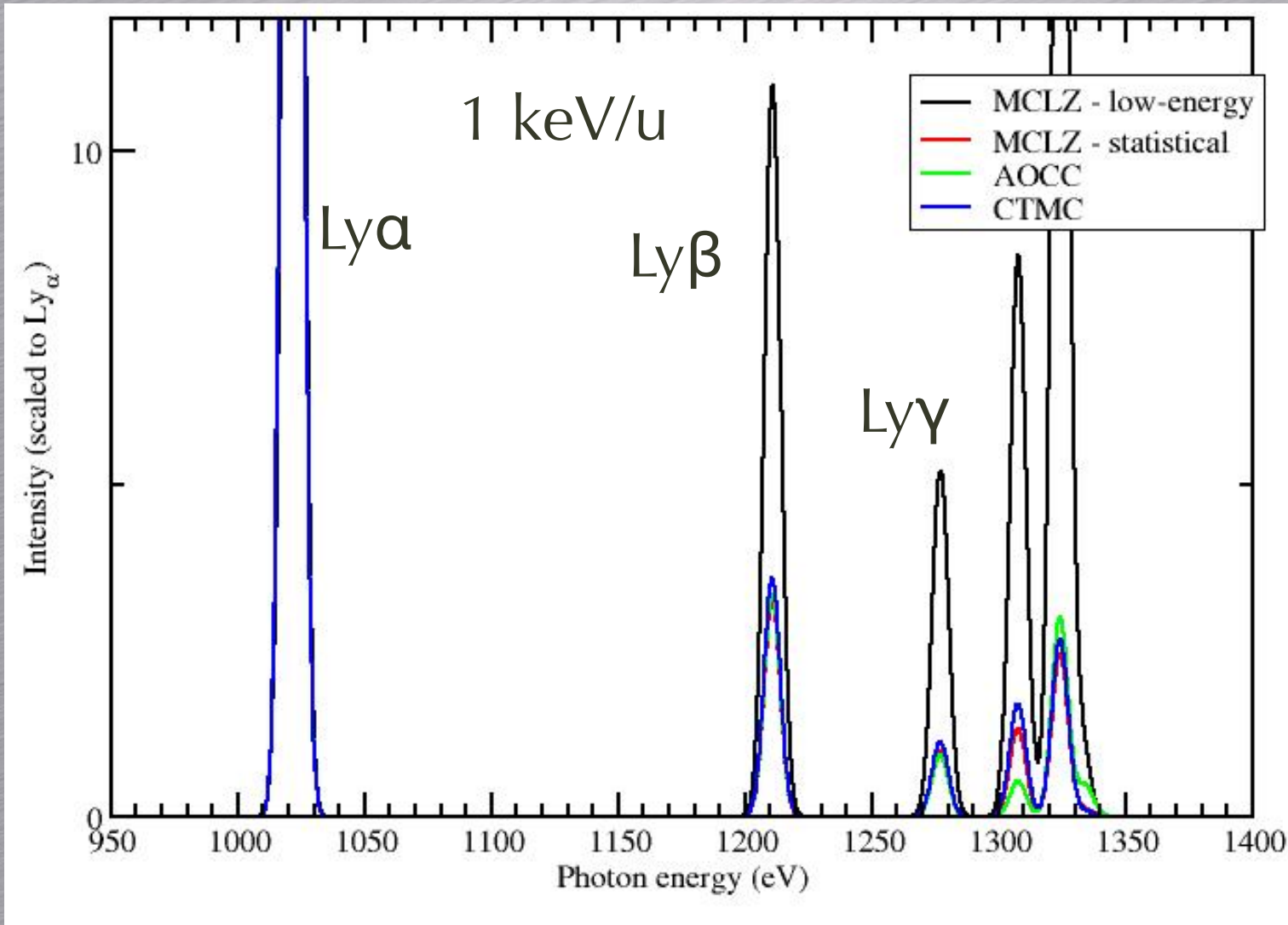
X-ray Spectra for O^{8+} + H comparison



4.5 eV
resolution

Cumbee et al.
(2019)

X-ray Spectra for Ne^{10+} + H comparison

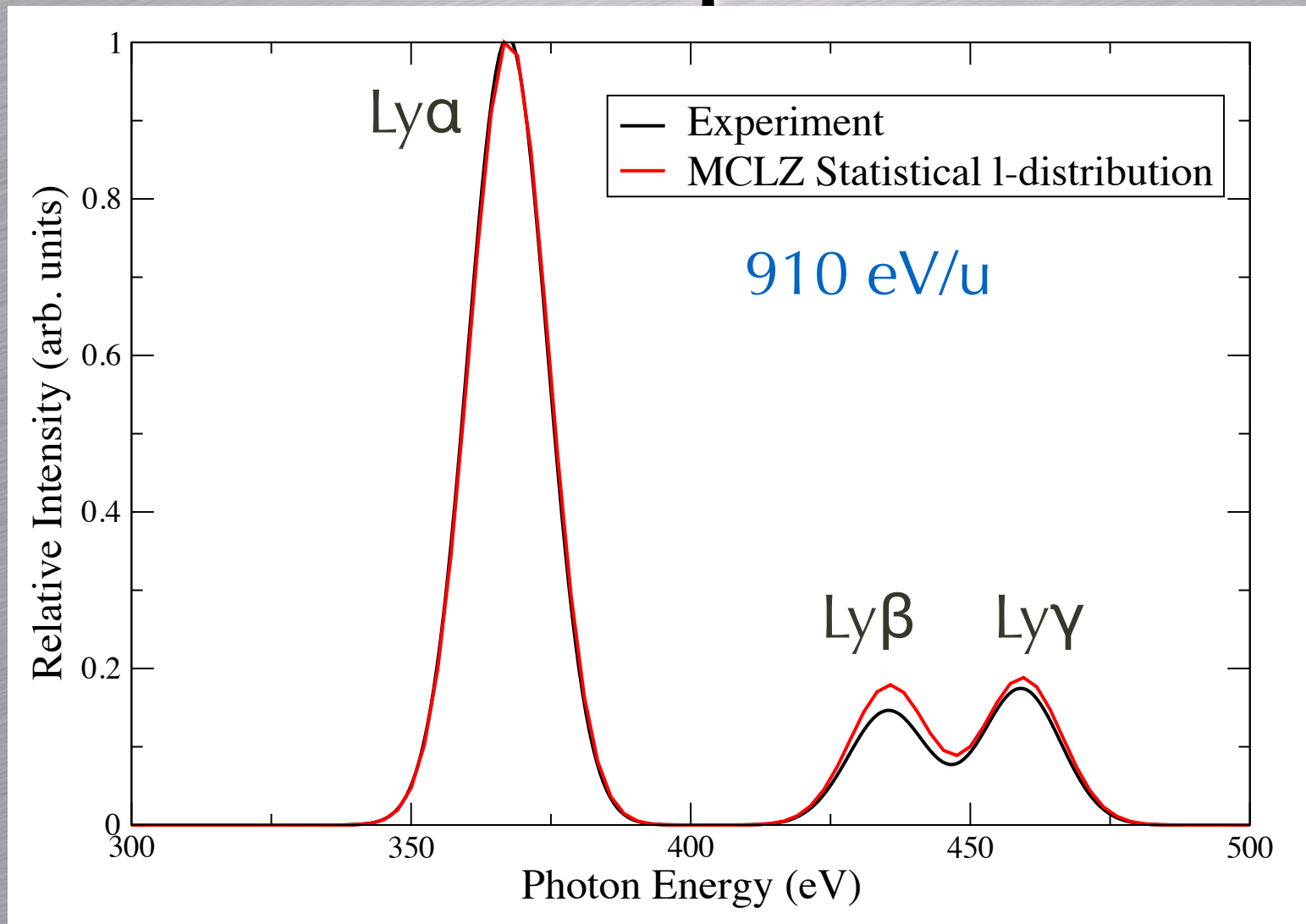


4.5 eV
resolution

Lyons et al.
(2016)
Cumbee et al.
(2016)

CTMC: Schultz & Krstic (1997); AOCC: Cumbee et al. (2016)

X-ray Spectra for $C^{6+} + H_2$ compared to experiment

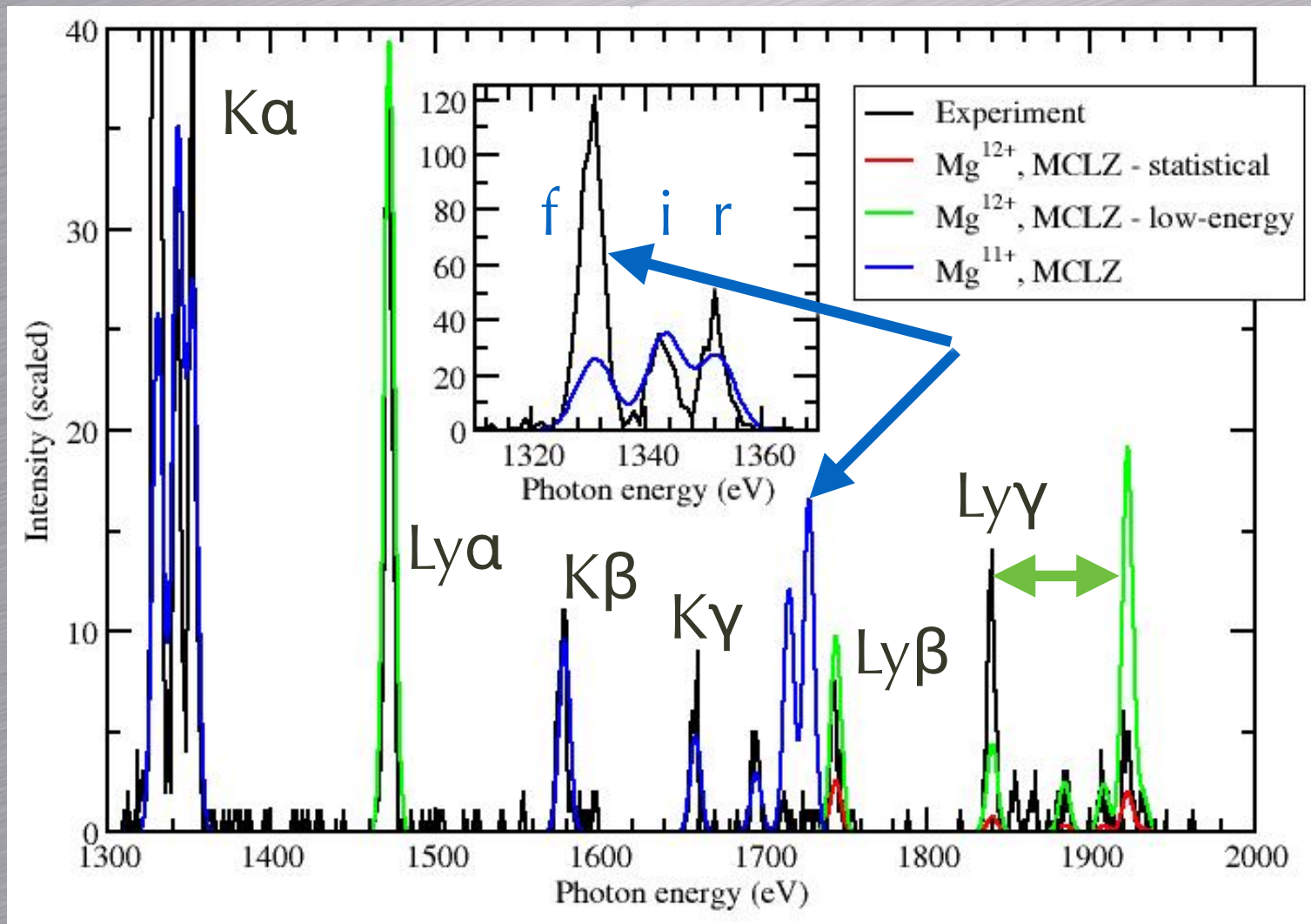


10 eV
resolution
Cumbee et al.
(2019)

Experiment: Fogle et al. 2014, PRA, 89, 042705

X-ray Spectra for Mg^{12+} and $\text{Mg}^{11+} + \text{H}_2$ compared to experiment

25 eV/u

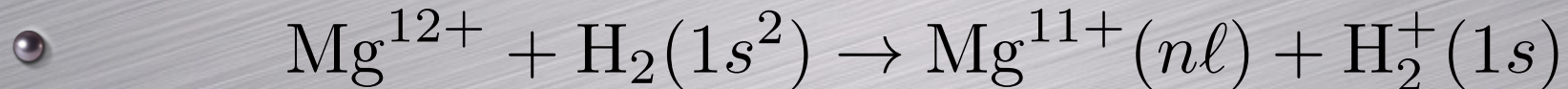


4.5 eV
resolution
Cumbee et al.
(2019)

Experiment: Betancourt-Martinez et al. 2014, PRA, 90, 052723

Double Electron Capture?

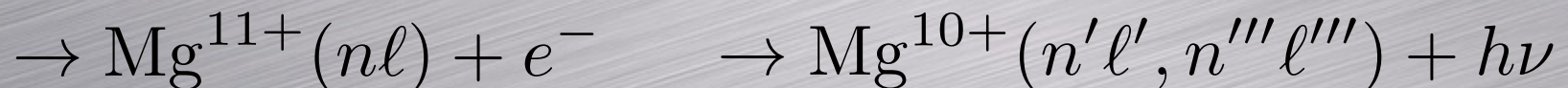
- Single Electron Capture (SEC)



- Double Electron Capture (DEC)



- Double Capture Autoionization (DCAI) or True DC (TDC)



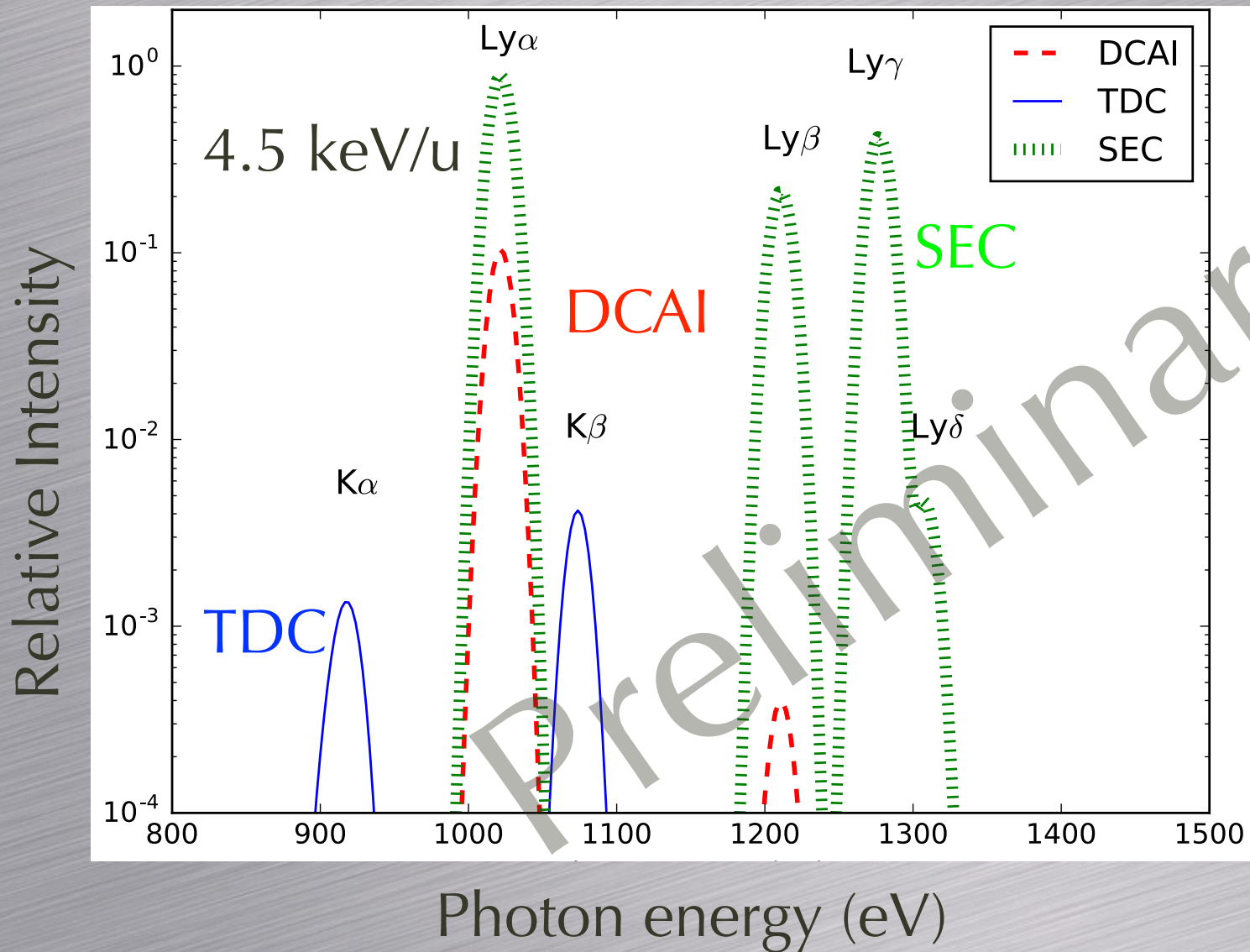
- SEC + DCAI = q,q-1

- Measurement is of q,q-1

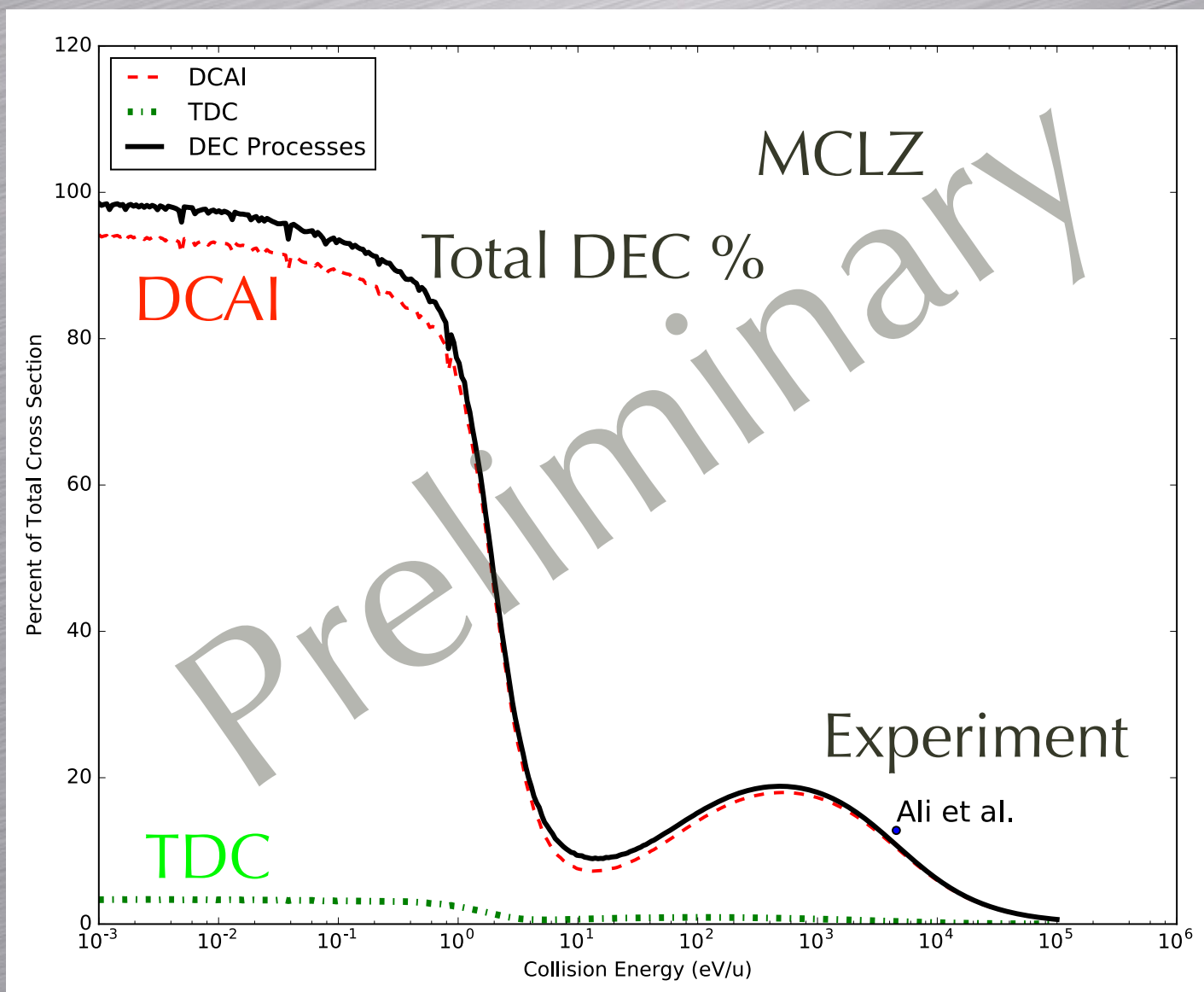
- Need Autoionization and Radiative Decay rates to determine branching ratios

Ne¹⁰⁺ + He

Spectrum Contributions

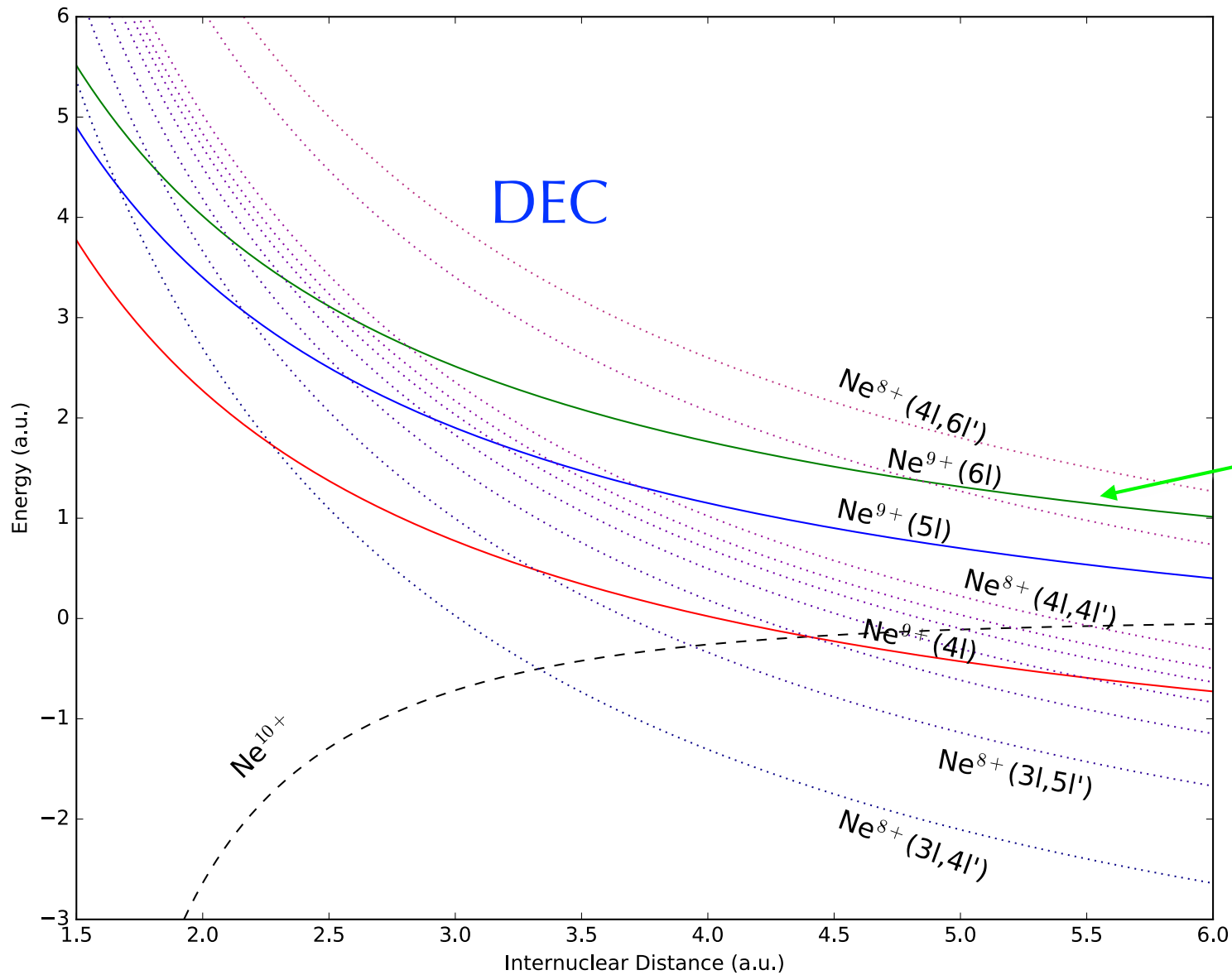


Ne¹⁰⁺ + He Double Capture Processes



Ne¹⁰⁺ + He

Empirical Potentials



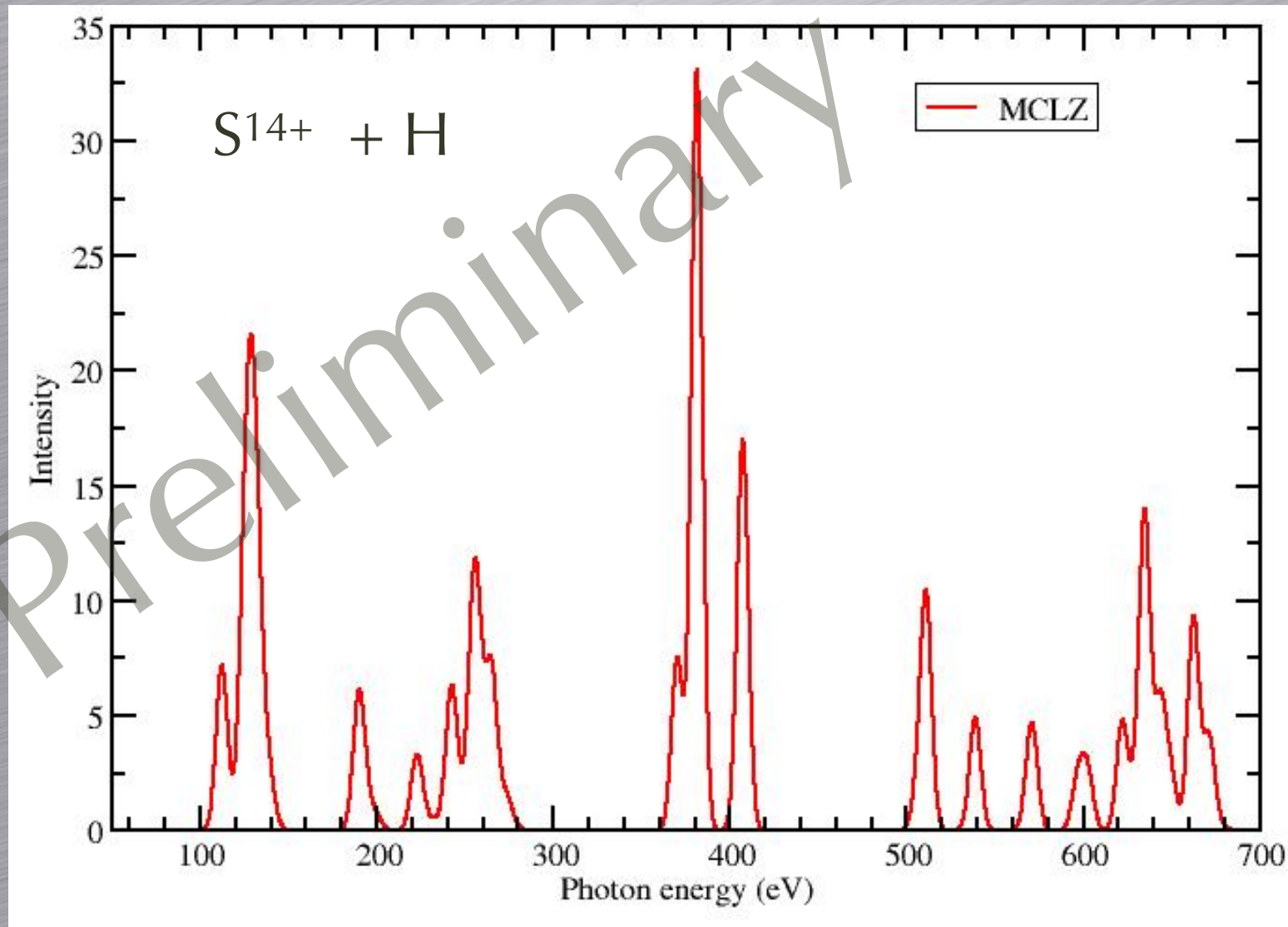
Ne¹⁰⁺ + He

Mg¹¹⁺ and Mg¹²⁺ discrepancies

- DCAI tends to populate lower n-values than SEC
- Suppresses high-n transition lines
- He-like ion measurement appears to have larger triplet population
- Should non-adiabatic coupling depend on spin?
- Topics to explore with joint Clemson-Auburn-GSFC-Livermore-UGA measurements focused on double-capture

Li-like S CX emission

MCLZ 1 keV/u



4.5 eV
resolution

Summary

- Reviewed Kronos database for CX X-ray emission - single electron capture only
- Most cross section data obtained with MCLZ method
- Some QMOCC, AOCC, CTMC, and prior recommended cross sections
- Includes more than 300 collision systems
- Dominant uncertainty in the potential difference at the avoided-crossings (R_x)

The Future

- New Kronos release coming soon
- Moving to multi-electron systems w/ MCLZ
- New QMOCC and AOCC codes in development
- Benchmarking to measurements
- Optimize LZ parameters with machine learning
- Double capture and fine-structure